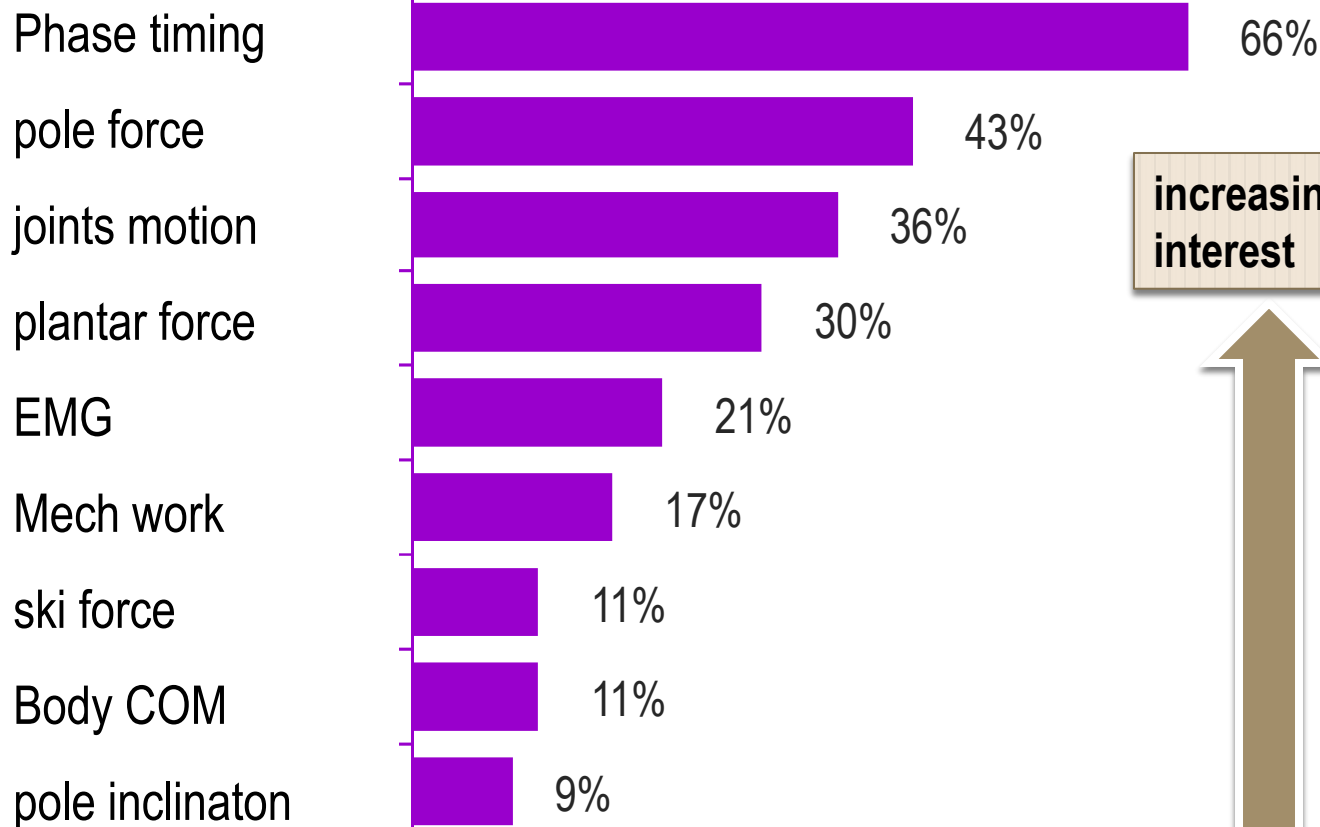


# Cross country skiing analyzed from center of mass point of view

**Pellegrini Barbara**  
**Zoppirolli Chiara**  
**Bortolan Lorenzo**  
**Schena Federico**

# Recent Cross country ski biomechanical studies

Biomechanical studies 2008 -2015 : n 47



increasing  
interest

increasing  
complexity

# Cross-country skiing biomechanics

.....many segments and parameters to look at!

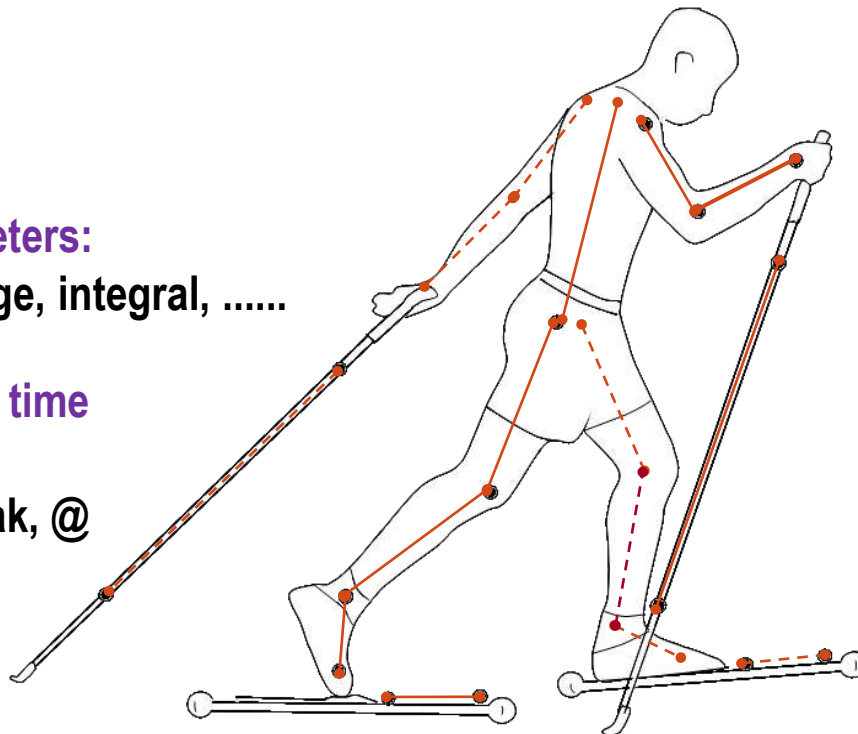


**Different parameters:**

Min, max, average, integral, .....

**Multiplied by N time  
instants :**

@ CT0%, @Fpeak, @  
v min....



# Cross-country skiing biomechanics

## .....many segments and parameters to look at!

*Med. Sci. Sports Exerc.*, Vol. 37, No. 5, pp. 807–818, 2005

### Biomechanical Analysis of Double Poling in Elite Cross-Country Skiers

HANS-CHRISTER HOLMBERG<sup>1,2</sup>, STEFAN LINDINGER<sup>3,4</sup>, THOMAS STÖGGL<sup>3,4</sup>, ERICH EITZLMAIR<sup>3,4</sup>, and ERICH MÜLLER<sup>3,4</sup>

EMG on 19 muscles

Pole force

Plantar force

Angle for 4 body joints

.....

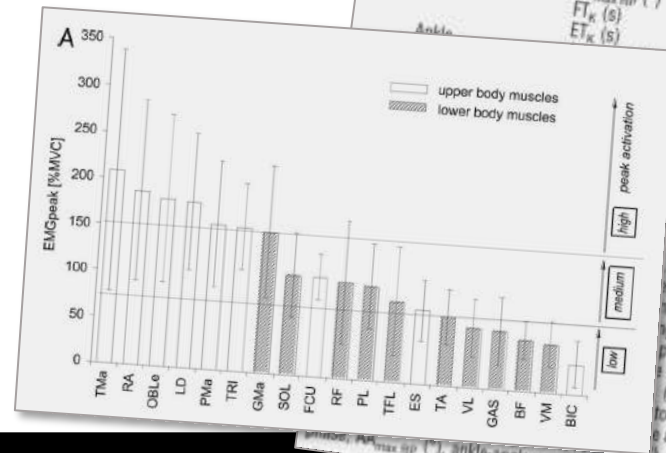


more than 60  
parameters have  
been extracted



TABLE 3. Kinematic cycle characteristics of DP at 85% of  $V_{max}$  ( $N = 11$ ), values mean  $\pm$  SD.

	Variables*	Mean $\pm$ SD
Elbow	EA <sub>start pp</sub> (°)	104 $\pm$ 19
	EA <sub>min pp</sub> (°)	69 $\pm$ 21
	EA <sub>end pp</sub> (°)	160 $\pm$ 10
	FT <sub>E</sub> (s)	0.09 $\pm$ 0.02
	ET <sub>E</sub> (s)	0.19 $\pm$ 0.02
Hip	AV <sub>E max pp</sub> (°·s <sup>-1</sup> )	370 $\pm$ 171
	HA <sub>start pp</sub> (°)	136 $\pm$ 14
	HA <sub>min pp</sub> (°)	101 $\pm$ 16
	HA <sub>end pp</sub> (°)	102 $\pm$ 17
	FT <sub>H</sub> (s)	170 $\pm$ 8
Knee	ET <sub>H</sub> (s)	0.13 $\pm$ 0.03
	AV <sub>H max pp</sub> (°·s <sup>-1</sup> )	0.69 $\pm$ 0.09
	KA <sub>start pp</sub> (°)	248 $\pm$ 76
	KA <sub>min pp</sub> (°)	150 $\pm$ 14
	KA <sub>end pp</sub> (°)	138 $\pm$ 14
Ankle	KA <sub>max pp</sub> (°)	141 $\pm$ 16
	FT <sub>K</sub> (s)	167 $\pm$ 6
	ET <sub>K</sub> (s)	0.15 $\pm$ 0.06
		0.82 $\pm$ 0.16
		86 $\pm$ 11



ling phase; EA<sub>min pp</sub> (°), elbow-angle  
gle at the end of poling phase; FT<sub>E</sub> (s),  
extension time elbow in poling phase;  
ion in poling phase; HA<sub>start pp</sub> (°), hip  
hip-angle minimum in poling phase;  
; HA<sub>max pp</sub> (°), hip-angle maximum in  
ing phase; ET<sub>H</sub> (s), extension time hip  
angular velocity of hip flexion in poling  
pole phase; KA<sub>min pp</sub> (°), knee-angle  
at the end of poling phase; KA<sub>max pp</sub>  
(s), flexion time knee during poling  
to KA<sub>max pp</sub>; AA<sub>min pp</sub> (°), ankle-angle  
at the end of poling phase

# Cross-country skiing biomechanics

## .....many segments and parameters to look at!

*Med. Sci. Sports Exerc.*, Vol. 37, No. 5, pp. 807–818, 2005

### Biomechanical Analysis of Double Poling in Elite Cross-Country Skiers

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EMG on 19 muscles

Pole force

Plantar force

Angle for 4 body joints

.....

“The best skiers use a DP strategy with specific characteristics directly correlated to DP velocity”

“This strategy is characterized by smaller joint angles, higher flexion velocities, and higher pole force applied during a shorter poling phase”



TABLE 3. Kinematic cycle characteristics of DP at 85% of  $V_{max}$  ( $N = 11$ ), values are mean  $\pm$  SD.

Variables <sup>a</sup>	Mean $\pm$ SD
<b>Elbow</b>	
EA <sub>start pp</sub> (°)	104 $\pm$ 19
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AV <sub>flex pp</sub> (°·s <sup>-1</sup> )	0.13 $\pm$ 0.03
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ET <sub>K</sub> (s)	141 $\pm$ 16
<b>Ankle</b>	
ET <sub>A</sub> (s)	167 $\pm$ 6
	0.15 $\pm$ 0.06
	0.82 $\pm$ 0.16
	86 $\pm$ 11
	96 $\pm$ 5
	0.19 $\pm$ 0.07
	95 $\pm$ 14
	105 $\pm$ 8

<sup>a</sup>EA<sub>min pp</sub> (°), elbow-angle of poling phase; ET<sub>E</sub> (s), elbow in poling phase; HA<sub>min pp</sub> (°), hip minimum in poling phase; HA<sub>max pp</sub> (°), hip-angle maximum in poling phase; ET<sub>H</sub> (s), extension time of hip flexion in poling phase; KA<sub>min pp</sub> (°), knee-angle minimum in poling phase; KA<sub>max pp</sub> (°), knee-angle maximum in poling phase; ET<sub>K</sub> (s), knee extension time during poling phase; ET<sub>A</sub> (s), ankle-angle minimum in recovery phase.



# Cross-country skiing biomechanics

## ..from many segments to body COM

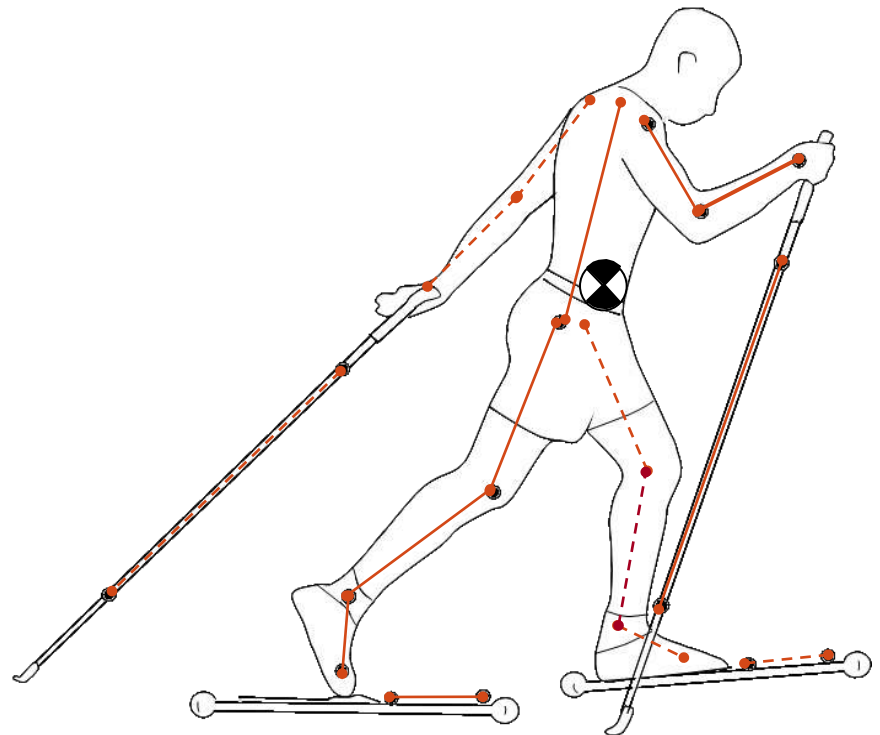
How to describe body motion  
in more..general and simplified way??



### Body COM

COM is the point at which the entire weight of a body may be considered as concentrated.

The resultant of all forces acting on the body can be considered as applied on COM.



# Cross-country skiing biomechanics

## ..from many segments to body COM

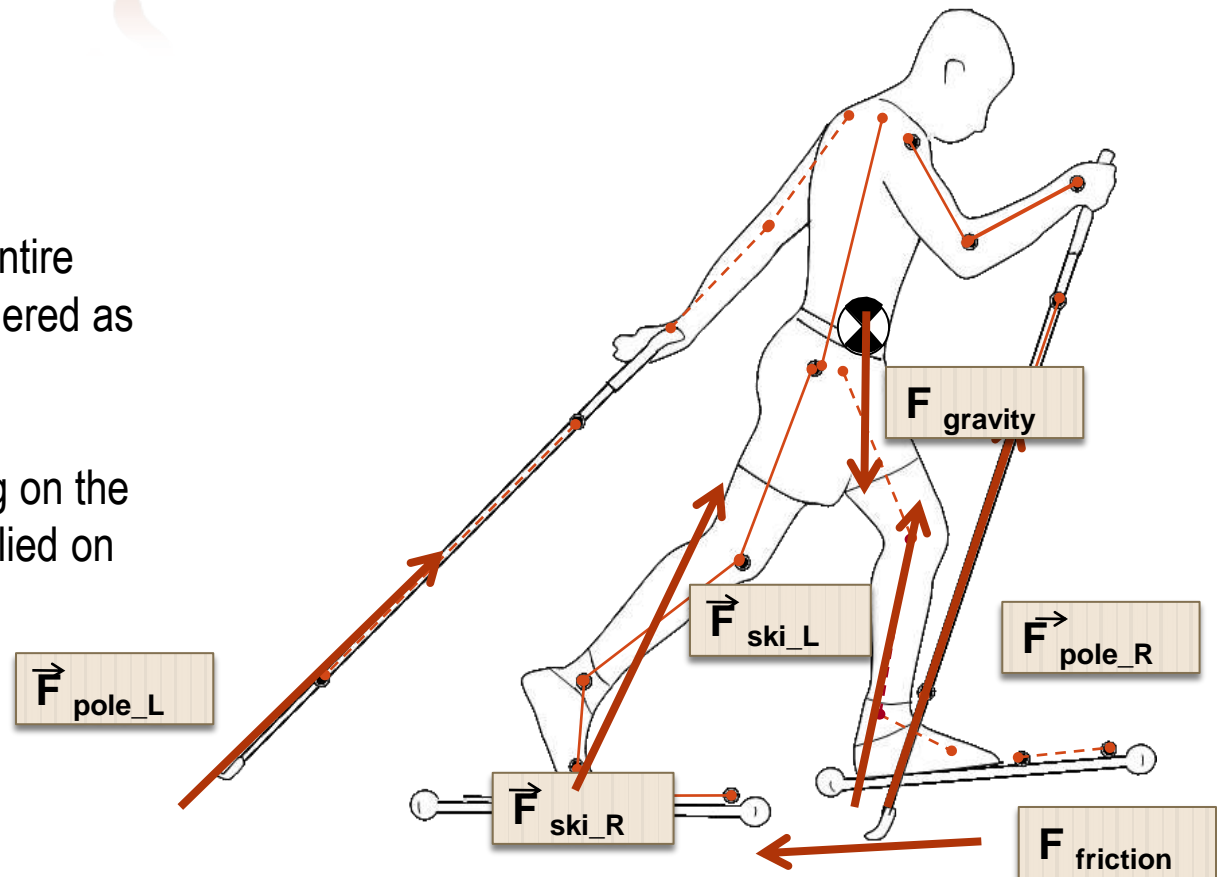
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# Cross-country skiing biomechanics

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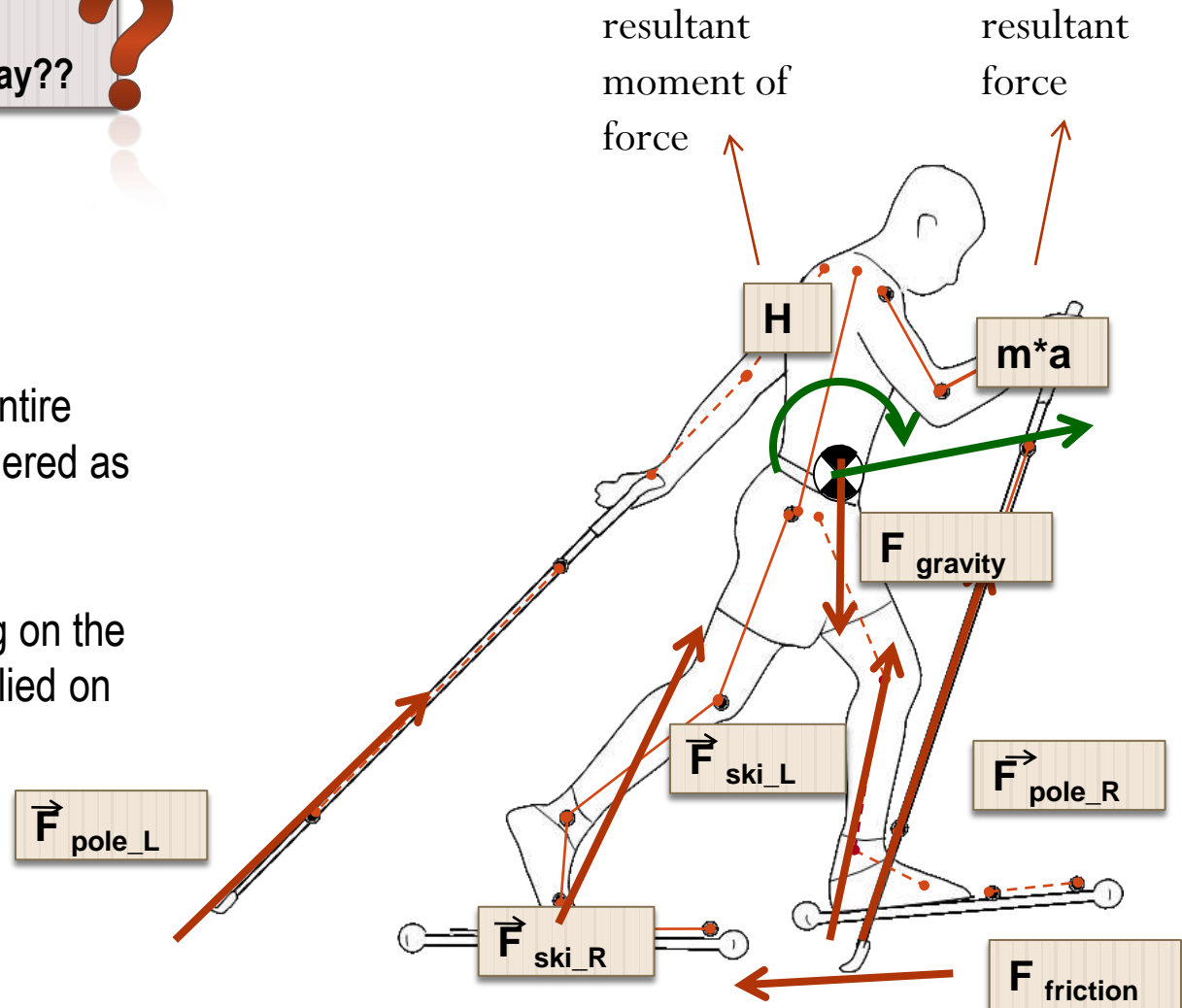
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# Cross-country skiing biomechanics

## ..from many segments to body COM

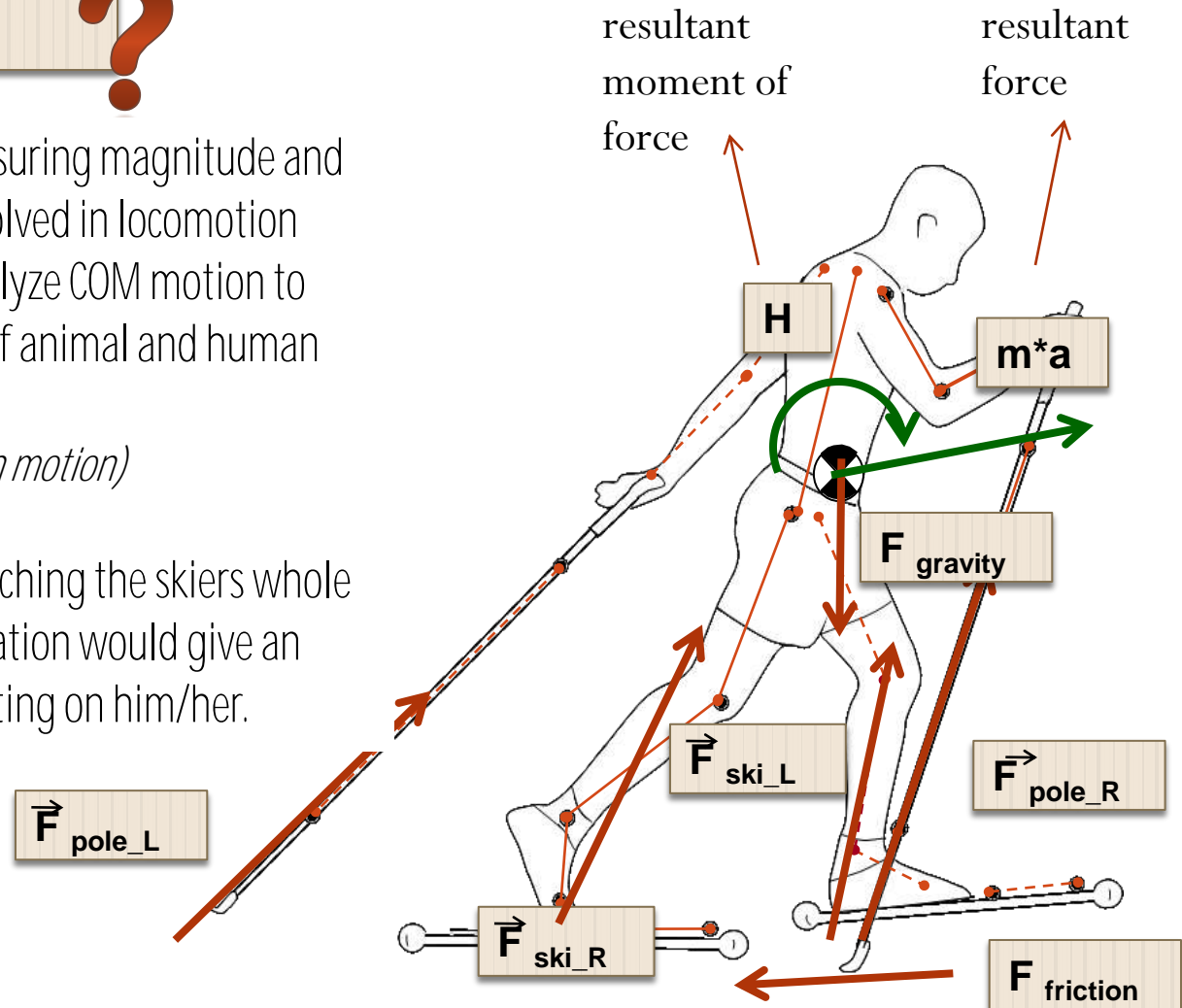
### Reasons to look at COM



The impossibility of directly measuring magnitude and point of application of forces involved in locomotion inspired many researchers to analyze COM motion to derive some mechanical aspect of animal and human movement

*(Zatsiorsky, 2000, Kinetics of human motion)*

Looking at COM, would mean catching the skiers whole motion and analyzing its acceleration would give an idea of the effect of the forces acting on him/her.



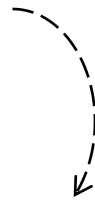
# body COM..a simplified view, not a simplified measurement

How to calculate body COM



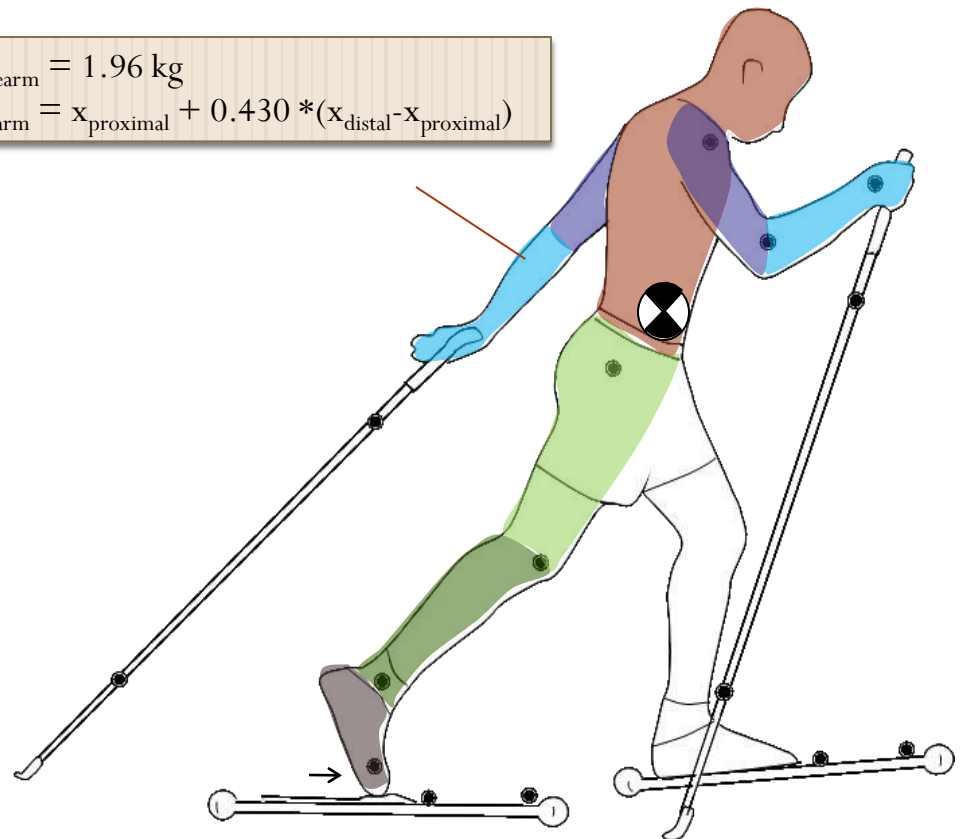
$$x_{COM} = \frac{\sum_i x_i m_i}{M}$$

$$y_{COM} = \frac{\sum_i y_i m_i}{M}$$



$$m_{\text{forearm}} = 1.96 \text{ kg}$$
$$x_{\text{forearm}} = x_{\text{proximal}} + 0.430 * (x_{\text{distal}} - x_{\text{proximal}})$$

Mass and center of mass position of each body segments are *approximated* and taken for anthropometric table  
(Dempster 1955, de Leva (1996))



# Measurements setup

## Roller skiing on the treadmill:

- no variability of environmental condition
- fixed and precise speed and slope
- many consecutives cycles

**Treadmill belt:** 2.5 m wide 3.5m long

**Poles:** various length

**Rollers skis:** Nord CL, ski skett

**Rolling friction coefficient:**  $\mu = 0.024$

comparable with other treadmills (Kwamme, 2005, Hoffman, 1995)  
and lower than typical on snow skiing  $\mu = 0.01 - 0.10$   
(Colbeck 1994)

Most published data on cross country skiing originated from roller skis studies on treadmill  
(Kwamme, 2005, Hoffman, 1990, Millet 1998, Mahood 2001, Holmberg 2005)



research center - Rovereto (TN)  
**CeRiSM**  
sport mountain health

locomotion lab

Double Poling - **DP**

Double Poling with kick - **DK** Diagonal Stride - **DS**

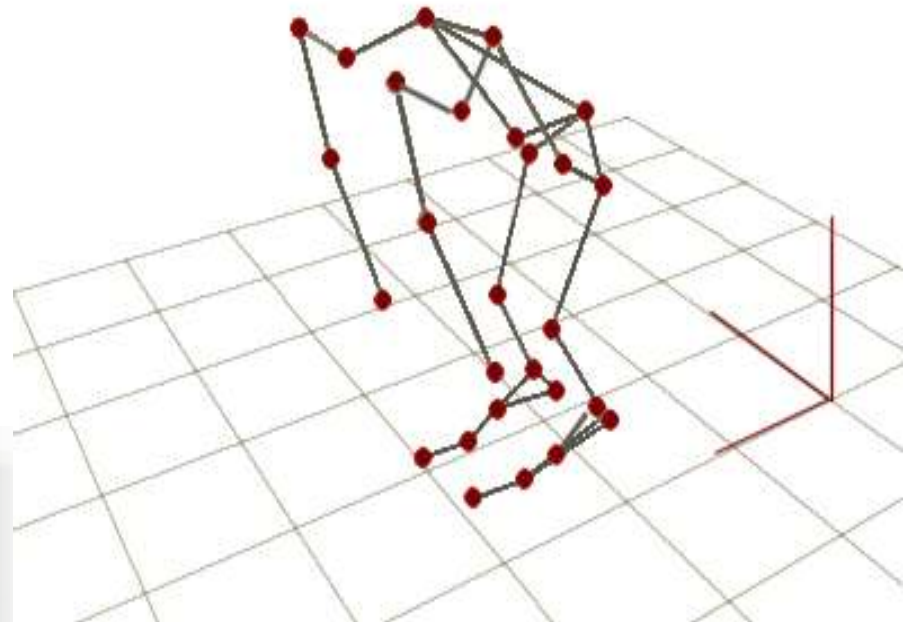


# Laboratory measurement - Motion Capture

6 infrared cameras (ProReflex, Qualisys)  
placed on both side acquiring 3D motion at 100Hz

2 markers on every pole and ski  
18 markers on body landmarks

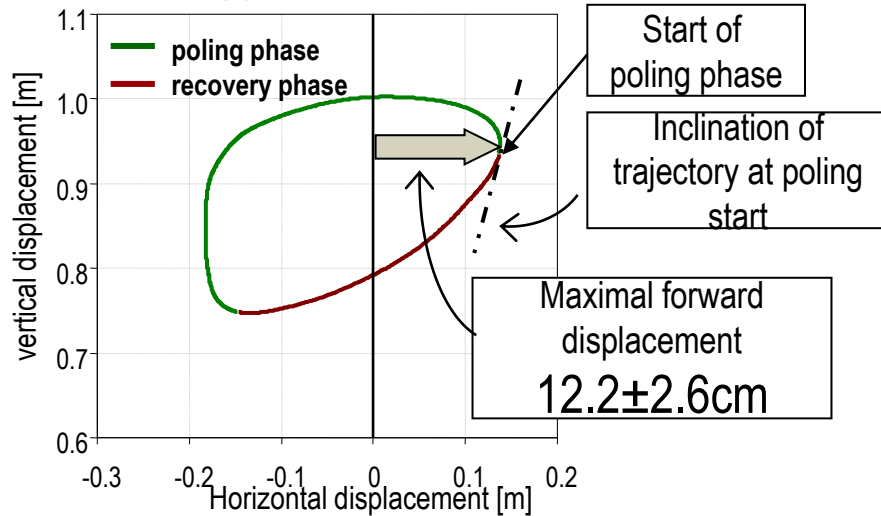
12 body segments + **pole and ski motion**



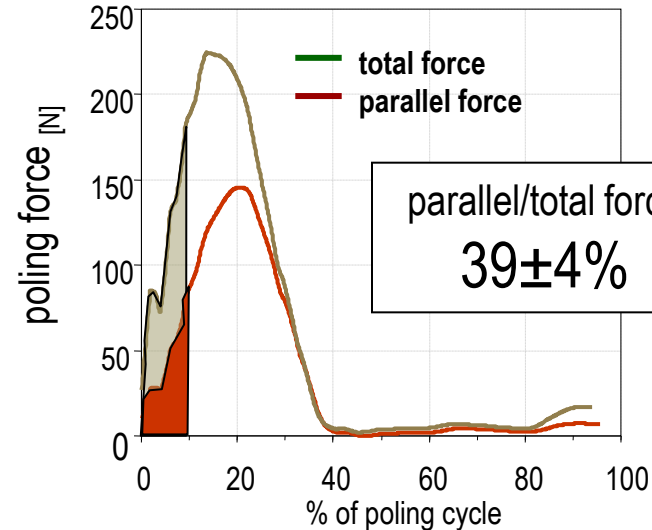
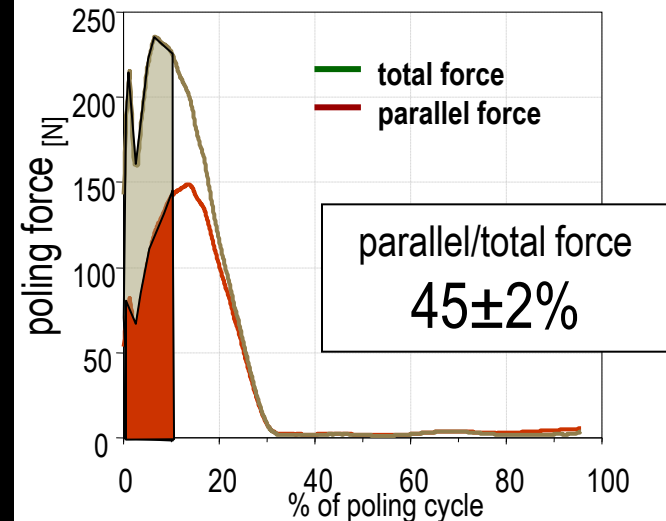
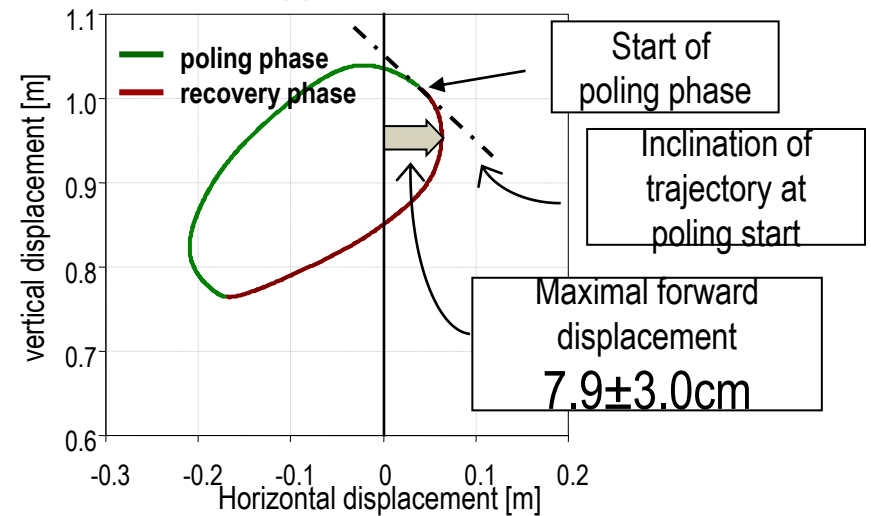


# Skiers body COM motion displacement

## Strategy A- 3 skiers

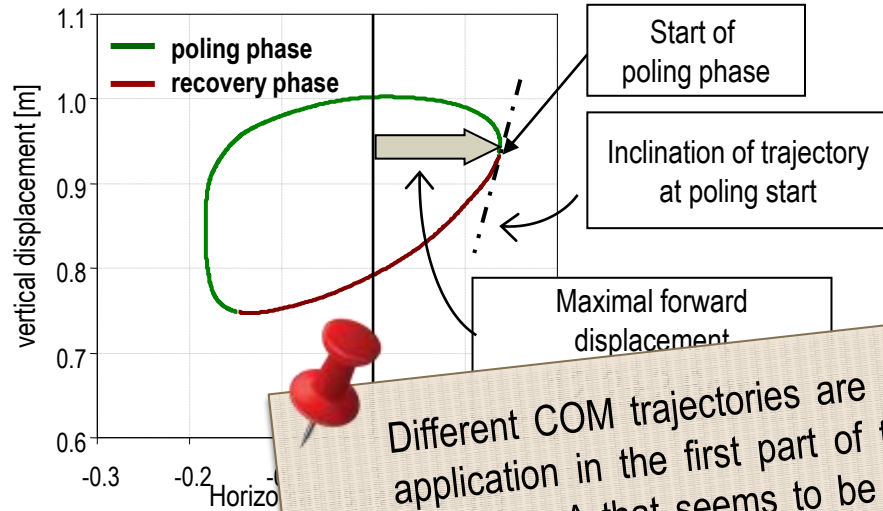


## Strategy B – 7 skiers

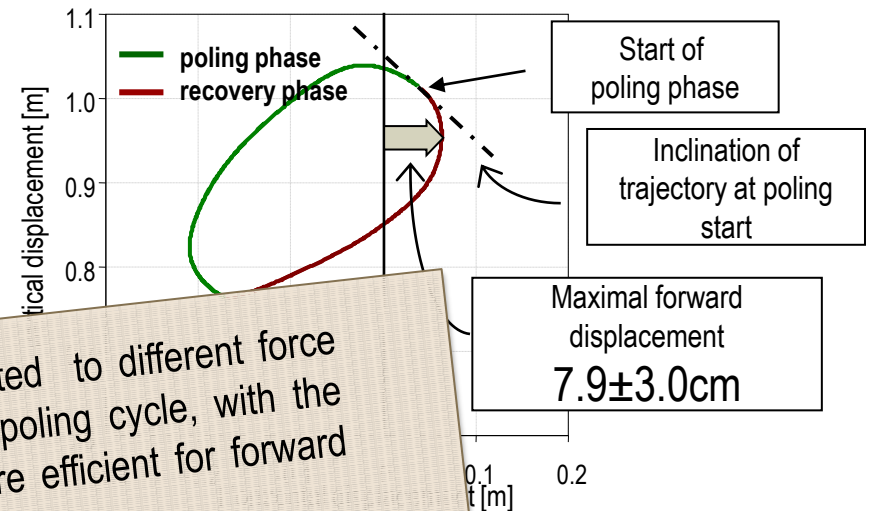


# Skiers body COM motion displacement

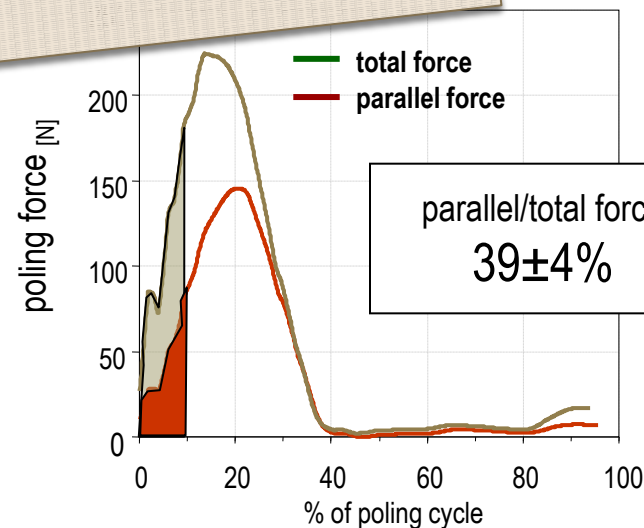
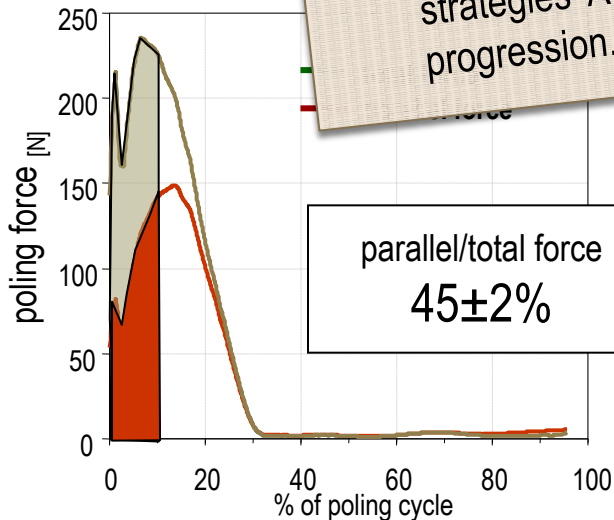
## Strategy A- 3 skiers



## Strategy B – 7 skiers



Different COM trajectories are related to different force application in the first part of the poling cycle, with the strategies A that seems to be more efficient for forward progression.



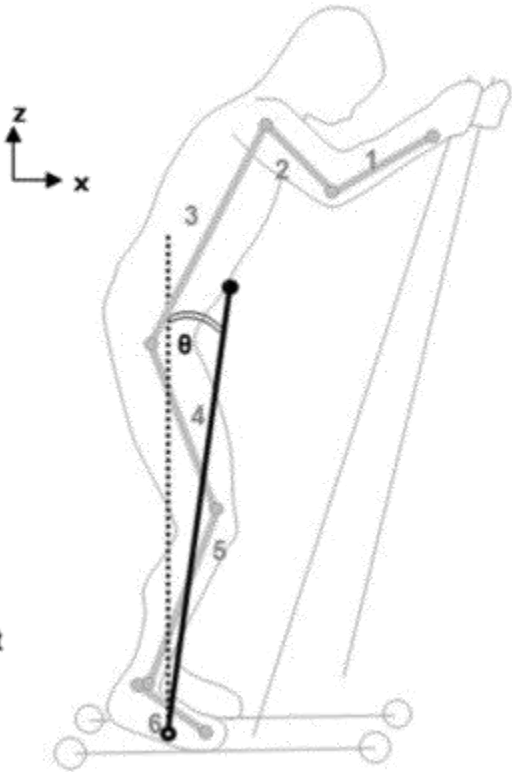
ORIGINAL ARTICLE

Energetics and biomechanics of double poling in regional and high-level cross-country skiers

Chiara Zoppirolli · Barbara Pellegrini ·  
Lorenzo Bortolan · Federico Schena

subjects	stature	body mass	VO <sub>2</sub> max
8 high level	1.81 ± 0.04 m	75.3± 5.8 kg	61.2 ± 2.1 mL min <sup>-1</sup>
8 regional level	1.79 ± 0.05 m	73.2 ± 5.8 kg	52.5 ± 3.9 mL min <sup>-1</sup>

- passive markers
- body segments
- centre of mass (COM)
- PIVOT point
- ..... vertical line passing through the PIVOT point
- line passing through COM and PIVOT point



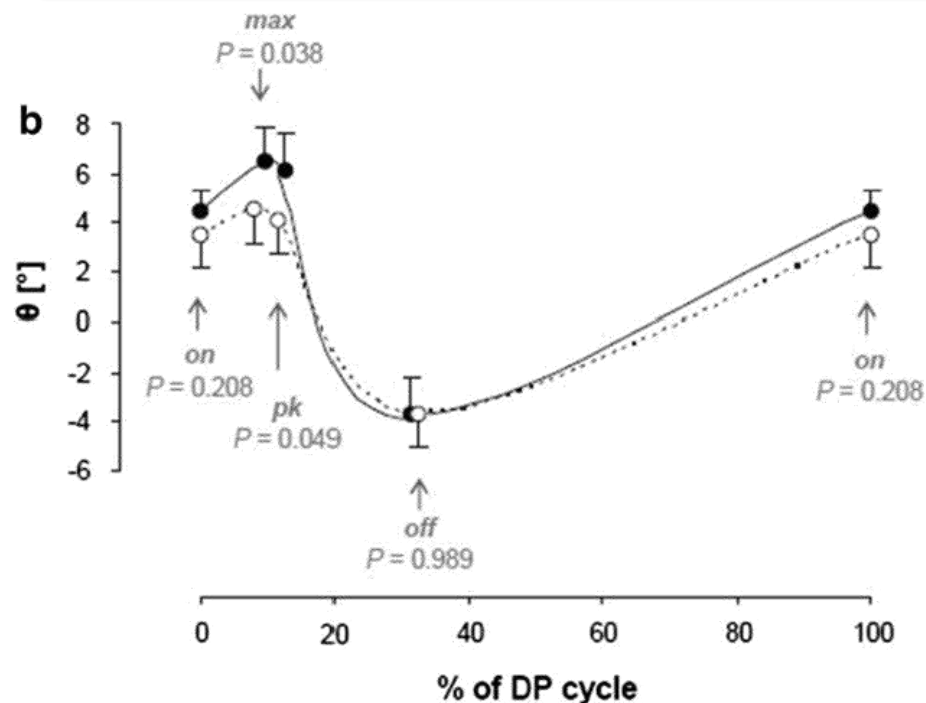
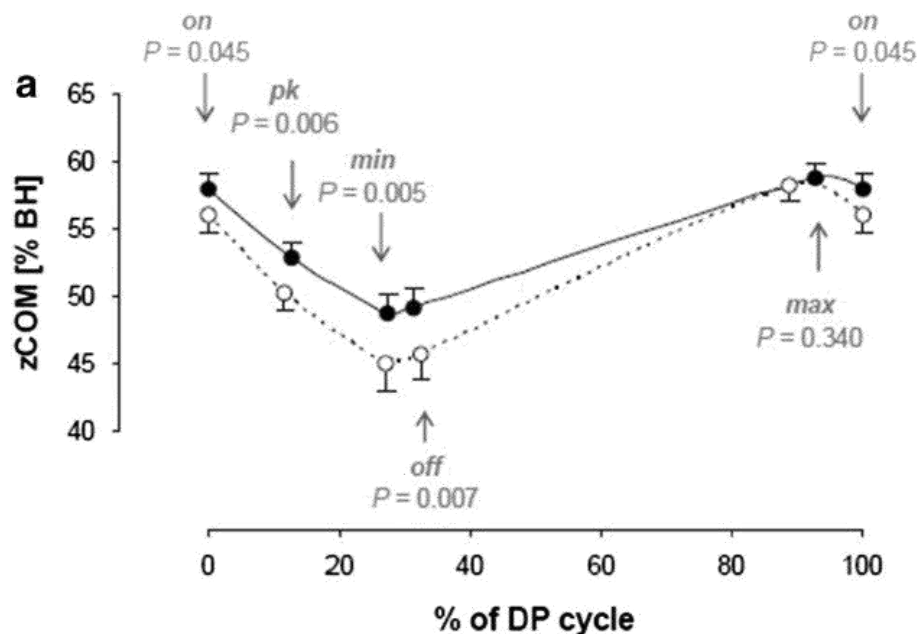


## Energetics and biomechanics of double poling in regional and high-level cross-country skiers

Chiara Zoppirolli · Barbara Pellegrini ·  
Lorenzo Bortolan · Federico Schena

“the **COM vertical displacement range** was significantly lower in high level group than in regional level group “

**Body forward inclination** at pole plant was significantly higher for high level skiers



## Energetics and biomechanics of double poling in regional and high-level cross-country skiers

Chiara Zoppirolli · Barbara Pellegrini ·  
Lorenzo Bortolan · Federico Schena

### Skiing economy

A forward multiple regression revealed that skiing economy was related to ( $\text{AdjR}^2 = 0.734$ ;  $P < 0.001$ ) )

- the maximum value of  $\theta$  ( $\theta_{\text{max}}$ )
- the minimum value of COM vertical displacement

Moreover,  $\theta_{\text{max}}$  positively related to poling force integrals and cycle duration ( $P < 0.05$ ).

### CONCLUSIONS:

A pronounced body inclination during the early poling phase and a reduced COM vertical displacement range concur in explaining the differences in skiing economy

A mechanically advantageous motion of COM during DP improves poling effectiveness, reduces cycle frequency and the mechanical work sustained

# The energy associated to COM motion

$$E_{COM} = Mgh_{COM} + \frac{1}{2}Mv_{COM}^2$$

PE

KE

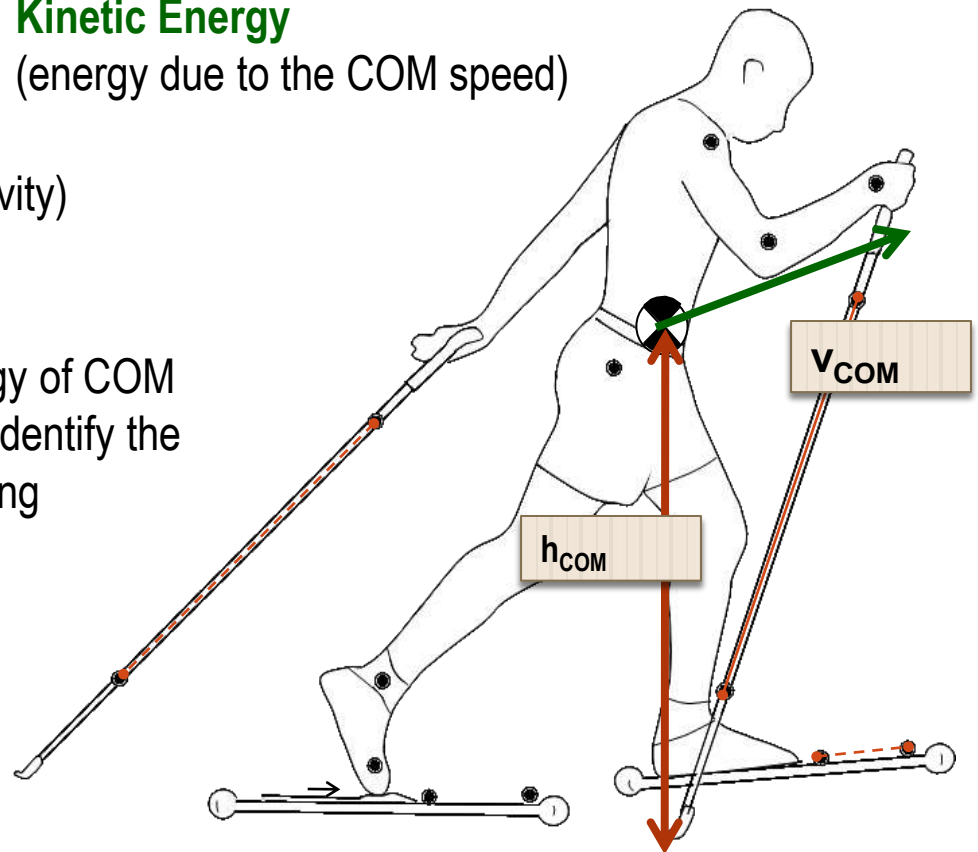
**Kinetic Energy**

(energy due to the COM speed)

**Potential energy**

(energy due to the COM position against gravity)

The analysis of the fluctuation of the energy of COM in cross country skiing can be adopted to identify the underlying mechanism of cross country skiing techniques



# ....from body COM to Energy...

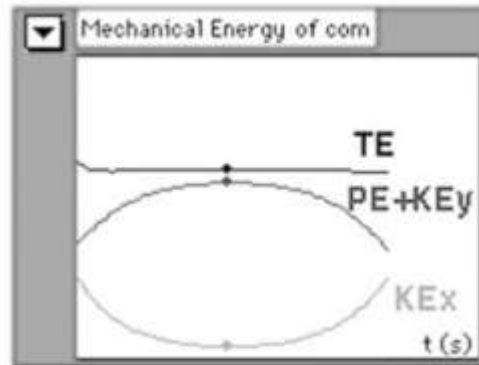
## Why to look at COM Energy



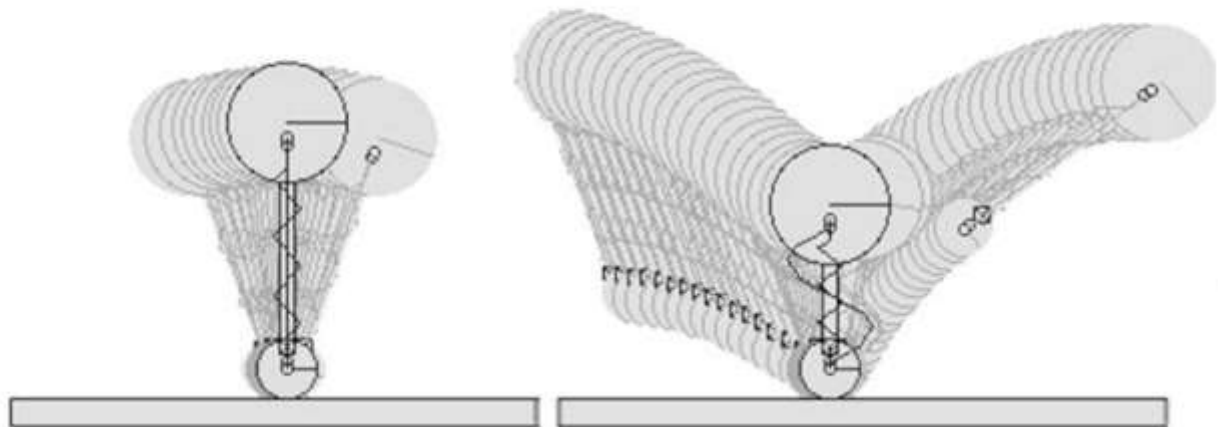
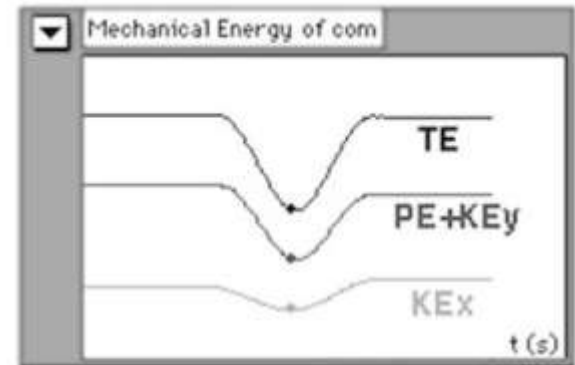
mechanical energy  
fluctuations can help in  
identifying the fundamental  
mechanisms that underlie  
terrestrial gait and to  
distinguish between different  
gait modes

It has been widely used in  
human and animal  
locomotion

*walking*



*running*



*Modified from Saibene and Minetti 2003*

# ....from Energy to Mechanical Work...

## The work energy principle

$$E_{COM} = Mgh_{COM} + \frac{1}{2} Mv_{COM}^2$$

PE KE

Sum of positive  
and negative  
changes of E

Sum of positive  
changes of E

**W<sub>ext,com</sub>**  
Works for moving COM

**W<sub>ext,com</sub>**  
Works for moving COM

classical definition of  
mechanical work:  
Work = Force X speed

when knowledge of force not  
always possible

calculation of  
mechanical work based  
on the changes of body  
energy



$$W_{\text{walking}} = W_{\text{environment}} + W_{\text{COM}} + W_{\text{int}}$$



$$W_{\text{running}} = W_{\text{environment}} + W_{\text{COM}} + W_{\text{int}}$$



$$W_{\text{cycling}} = W_{\text{environment}} + W_{\text{COM}} + W_{\text{int}}$$



$$W_{\text{skiing}} = W_{\text{environment}} + W_{\text{COM}} + W_{\text{int}}$$

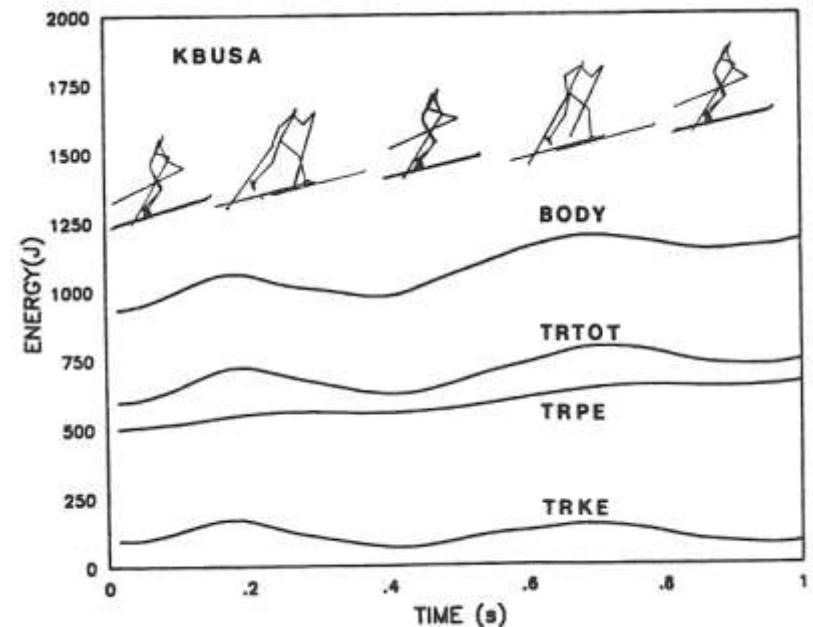
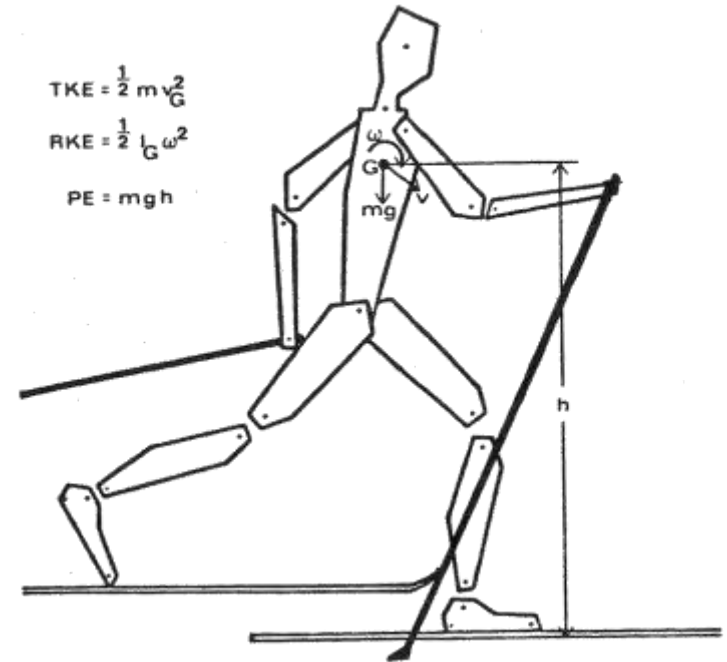
*Cavagna, G. A. J. Physiol (1969)  
di Prampero, P. E. (1986)  
Willems, P. A., Cavagna, G. A., & Heglund, N. C. (1995)  
Francescato MP, Girardis M, di Prampero PE. (1995)*

# Mechanical Power Output and Estimated Metabolic Rates of Nordic Skiers During Olympic Competition

*Robert Norman, Sylvia Ounpuu,  
Margo Fraser, and Ronald Mitchell*

"We have chosed .....to include not only phases of increasing energy level in the total work output estimate but to add the absolute value of the reductions in the energy level"

This may produce an overestimated of the mechanical power output. Ignoring the negative work will porduce and underestimate. The reality is somewhere in between

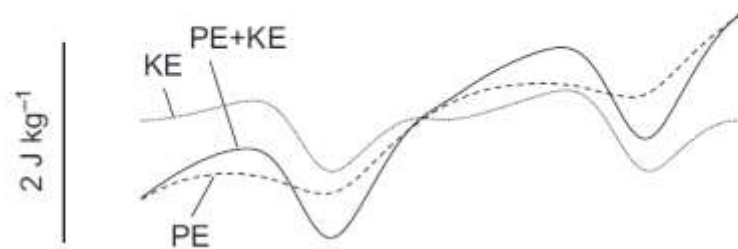
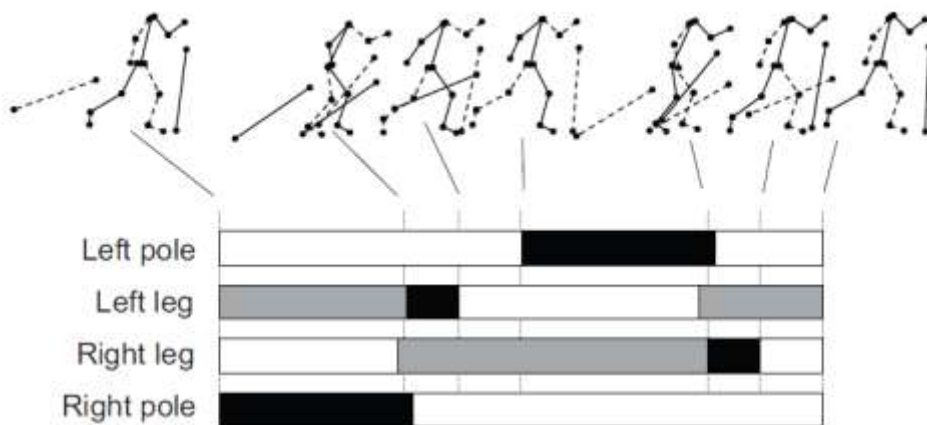


## RESEARCH ARTICLE

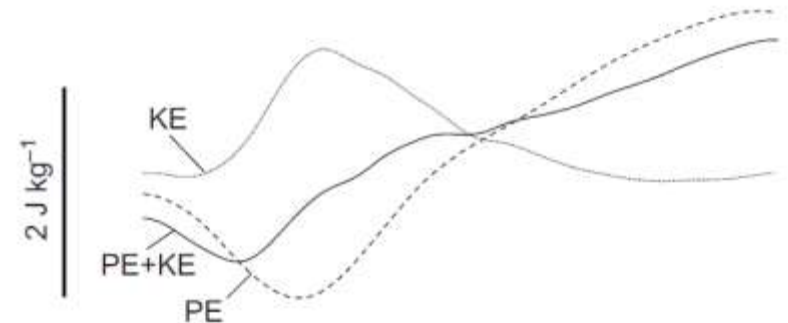
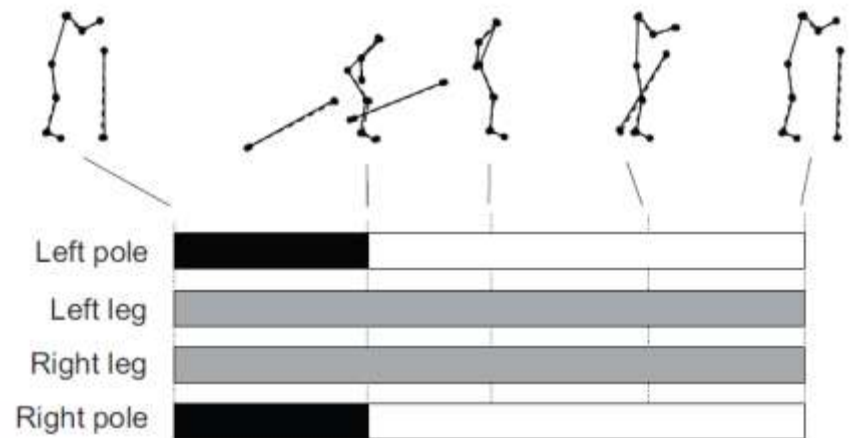
# Gait models and mechanical energy in three cross-country skiing techniques

Barbara Pellegrini<sup>1,2,\*</sup>, Chiara Zoppirolli<sup>1,2</sup>, Lorenzo Bortolan<sup>1,2</sup>, Paola Zamparo<sup>2</sup> and Federico Schena<sup>1,2</sup>

### Diagonal stride



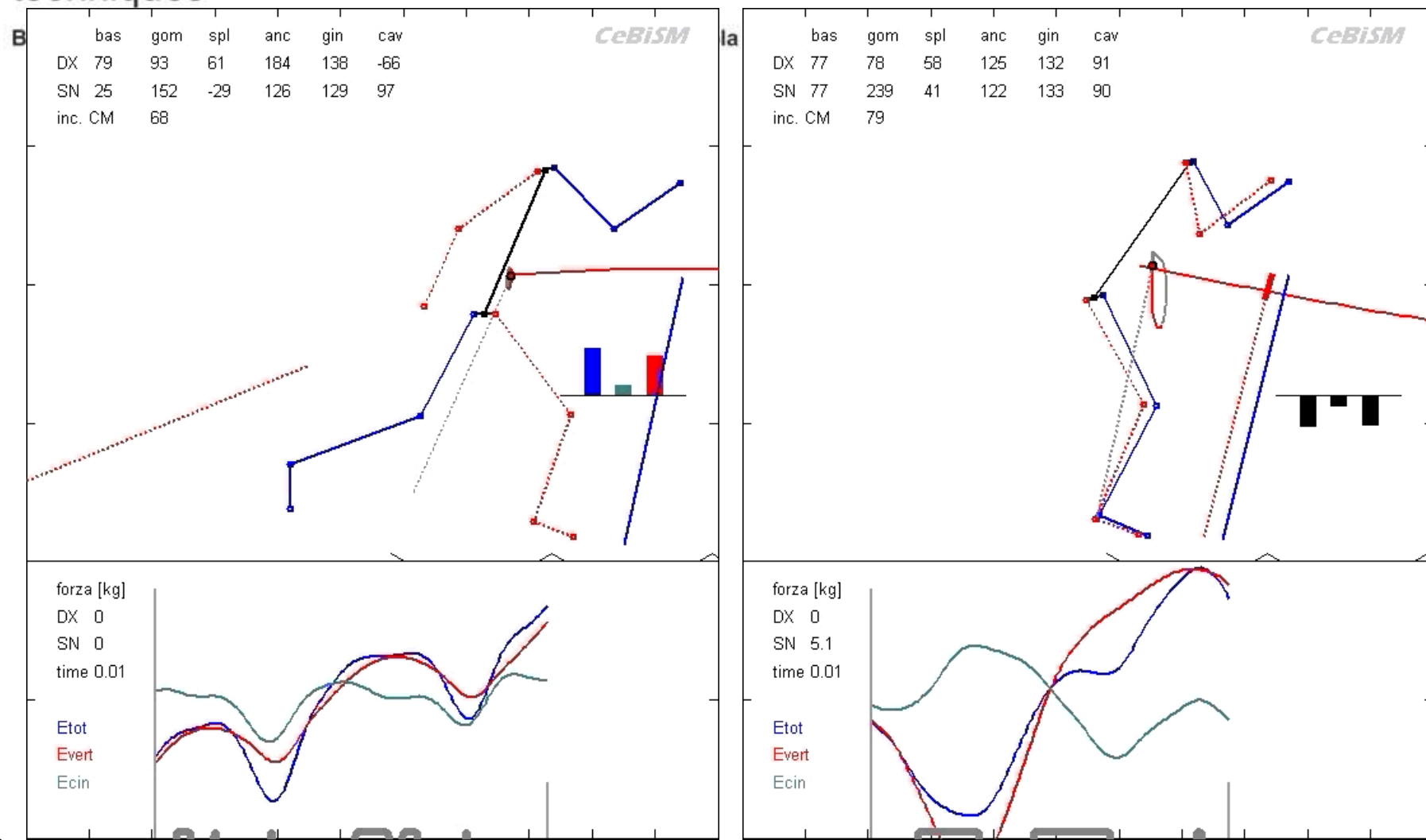
### Double poling





## RESEARCH ARTICLE

# Gait models and mechanical energy in three cross-country skiing techniques

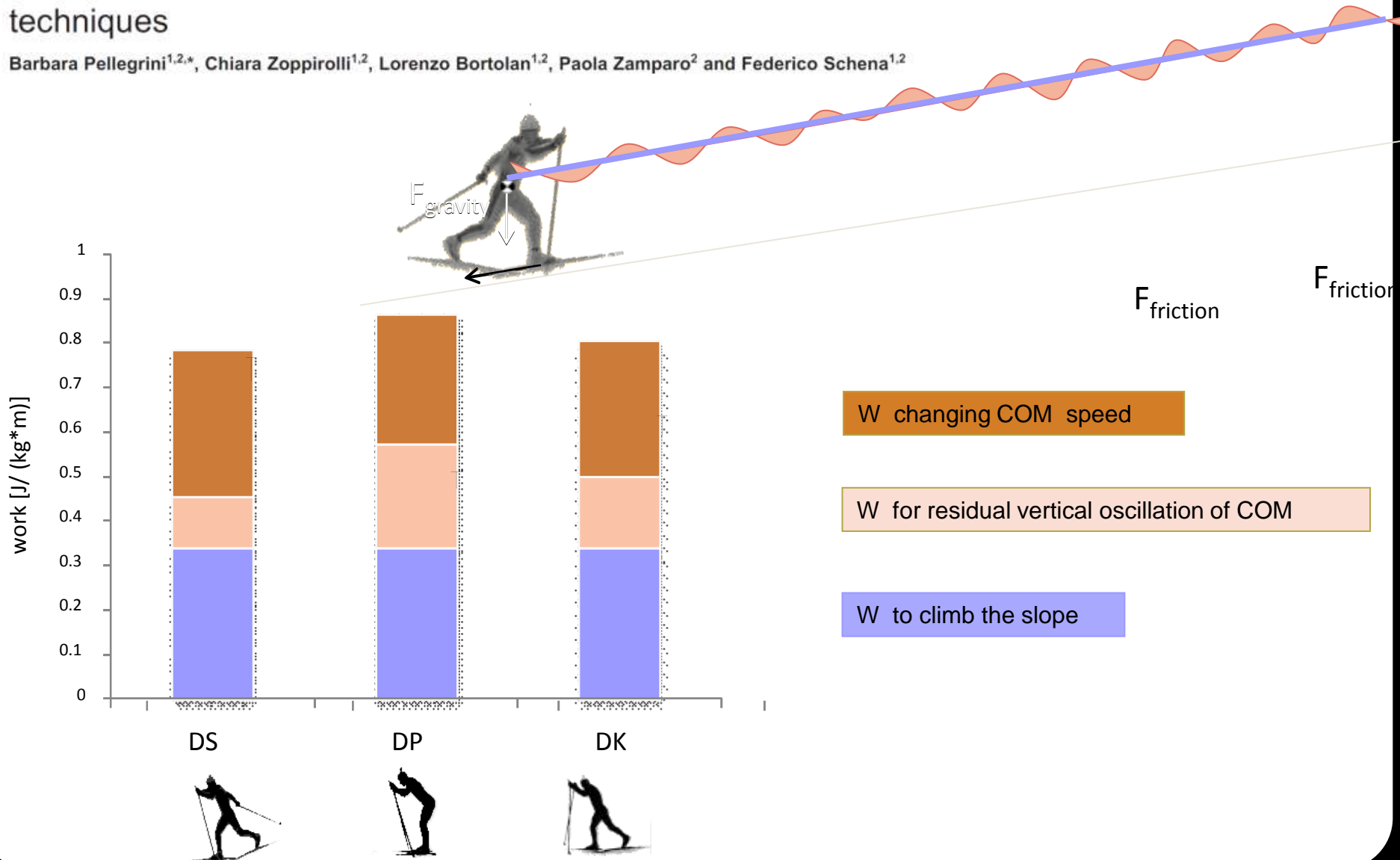


RESEARCH ARTICLE

# ..from Energy to mechanical Work...

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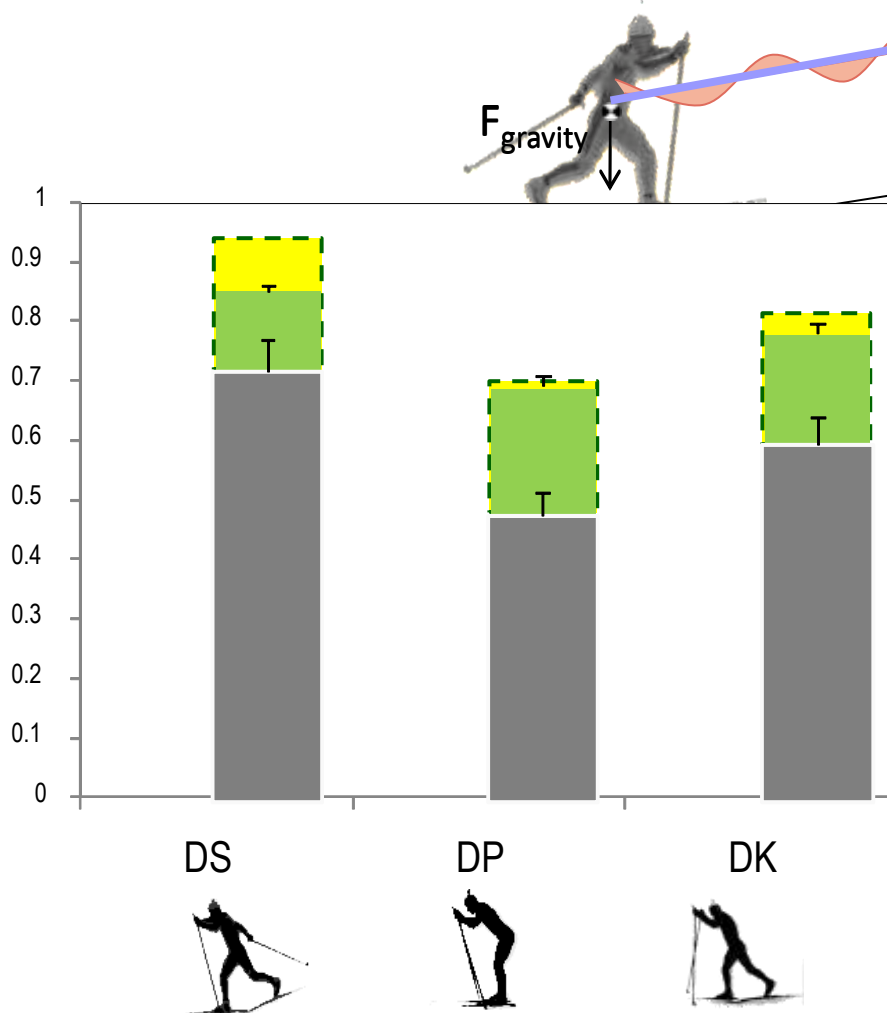


RESEARCH ARTICLE

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W for friction - estimation

W for friction – exact calculation

distance covered by rolling on skis/total distance travelled

DP = 100% DS = 41% DK = 83%

the frictional work calculated by considering the instantaneous values of speed and load on the skis, is 68% for DS and 86%, for DP of that estimated

# In conclusion



By analyzing the movement of the center of mass we can have an idea of the effects of the forces applied on a skier and their subsequent translation into movement and velocity



Determination of body COM requires:

- Measurements of all forces
- or
- Measurements of movements of all segments



Fluctuations of body COM can give insight in cross country skiing as gait modes




Calculation of mechanical work from energy fluctuations could add information in determining



Calculation of mechanical works requires to drawn assumption on unknown mechanisms, the results are estimation, may differ from true values

# Cross country skiing analyzed from center of mass point of view



**Pellegrini Barbara**  
**Zoppirolli Chiara**  
**Bortolan Lorenzo**  
**Schena Federico**

